## CH2303 Chemical Engineering Thermodynamics I

## Unit - III

## PVT Behavior of Fluids

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Figure 3.2: Sketch of experiment in which heat is added isobarically to water in a closed piston-cylinder arrangement.

$\square$


S3n

$537$

$53 n$

PVT surface for a substance that contacts upon freezing


S3n


Triple point: $\mathrm{P}=611.7 \mathrm{~N} / \mathrm{m}^{2} ; \mathrm{T}=0.01^{\circ} \mathrm{C}$
Critical point: $\mathrm{P}=220.64 \times 10^{5} \mathrm{~N} / \mathrm{m} 2 ; \mathrm{T}=374^{\circ} \mathrm{C}$
Normal boiling point: $100^{\circ} \mathrm{C}$; Normal freezing point: $0^{\circ} \mathrm{C}$ (1 atm)


## $537$



Temperature




p.



S3n

Percenlage of error
( $\left[1 v_{\text {tatle }}-v_{\text {icceal }} l / v_{\text {table }}\right] \times 100$ ) involved in assuming steam to be an ideal gas, and the region where steam can be treated as an ideal gas with less than 1 percent error.


## Comparison of ideal and van der Waals gas

Ideal gas
isotherm

van der Waals gas
isotherm

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Energy Input

## van der Waals Equation

$$
P=\frac{R T}{V-b}-\frac{a}{V^{2}}
$$

- The parameter $\mathbf{b}$ is related to the size of each molecule. The volume that the molecules, have to move around in is not just the volume of the container $\mathbf{V}$, but is reduced to $(\mathbf{V}-\mathbf{b})$.
- The parameter a is related to intermolecular attractive force between the molecules, and $1 / \mathbf{V}$ is the density of molecules. The net effect of the intermolecular attractive force is to reduce the pressure for a given volume and temperature.
- When the density of the gas is low (i.e., when $1 / \mathbf{V}$ is small and $\mathbf{b}$ is small compared to $\mathbf{V}$ ) the van der Waals equation reduces to that of the ideal gas law.


## van der Waals Constants

| Substance | $\mathbf{a}$ <br> $\left(\mathrm{J} \cdot \mathrm{m}^{3} / \mathrm{mole}^{2}\right)$ | $\mathbf{b}$ <br> $\left(\mathrm{m}^{3} / \mathrm{mole}\right)$ | $\mathbf{P}_{\mathbf{c}}$ <br> $(\mathrm{MPa})$ | $\mathbf{T}_{\mathbf{c}}$ <br> $(\mathrm{K})$ |
| :--- | :--- | :--- | :--- | :--- |
| Air | 1.1358 | $3.64 \times 10^{-5}$ | 3.77 | 133 |
| Carbon Dioxide $\left(\mathrm{CO}_{2}\right)$ | 1.3643 | $4.27 \times 10^{-5}$ | 7.39 | 304.2 |
| Nitrogen $\left(\mathrm{N}_{2}\right)$ | 1.1361 | $3.85 \times 10^{-5}$ | 3.39 | 126.2 |
| Hydrogen $\left(\mathrm{H}_{2}\right)$ | 1.0247 | $2.65 \times 10^{-5}$ | 1.30 | 33.2 |
| Water $\left(\mathrm{H}_{2} \mathrm{O}\right)$ | 1.5507 | $3.04 \times 10^{-5}$ | 22.09 | 647.3 |
| Ammonia $\left(\mathrm{NH}_{3}\right)$ | 1.4233 | $3.73 \times 10^{-5}$ | 11.28 | 406 |
| Helium $(\mathrm{He})$ | 1.00341 | $2.34 \times 10^{-5}$ | 0.23 | 5.2 |
| Freon $\left(\mathrm{CCl}_{2} \mathrm{~F}_{2}\right)$ | 1.0780 | $9.98 \times 10^{-5}$ | 4.12 | 385 |

Observe that inert gases like Helium have a low value of a as one would expect since such gases do not interact very strongly, and that large molecules like Freon have large values of $\mathbf{b}$.


Fig. 26.2 Isotherms of the van der Waals gas. Isotherms towards to the top right of the graph correspond to higher temperatures. The dashed line shows the region in which liquid and vapour are in equilibrium (see the end of Section 26.1). The thick line is the critical isotherm and the dot marks the critical point.






Comparison of actual behavior during isothermal compression to prediction of van der Waals equation.


An isotherm of the van der Waals equation for $\mathrm{T}<\mathrm{Tc}$.

## van der Waals Equation

$$
\begin{equation*}
\left(P+\frac{a}{V^{2}}\right)(V-b)=R T \tag{2.1}
\end{equation*}
$$

where $P=$ Pressure of the fluid
$V=$ Volume of the container for containing one mole the fluid
$a=$ correction term for pressure to account for the intermolecular forces of attraction
$b=$ correction term for voitiane to account for the volume of molecules
$R=$ Universal gas constant
$T=$ Absolute temperature.
Eqn.(2.1) can be written as

$$
\begin{equation*}
P=\frac{R T}{V-b}-\frac{a}{V^{2}} \tag{2.2}
\end{equation*}
$$

At the critical conditions $\left(T_{c}, P_{c}, V_{c}\right)$

$$
\begin{align*}
\left(\frac{\partial P}{\partial V}\right)_{T_{c}} & =0  \tag{2.3a}\\
\left(\frac{\partial^{2} P}{\partial V^{2}}\right)_{T_{c}} & =0 \tag{2.3b}
\end{align*}
$$

Taking derivative of Eqn.(2.2) with respect to $V$ at constant $T$, i.e.,

$$
\begin{equation*}
\left(\frac{\partial P}{\partial V}\right)_{T}=\frac{-R T}{(V-b)^{2}}+\frac{2 a}{V^{3}} \tag{2.4}
\end{equation*}
$$

Using Eqn.(2.3a), Eqn.(2.4) becomes,

$$
\begin{equation*}
\frac{-R T_{c}}{\left(V_{c}-b\right)^{2}}+\frac{2 a}{V_{c}^{3}}=0 \tag{2.5}
\end{equation*}
$$

Taking second derivative of Eqn.(2.2) with respect to $V$ at constant $T$ and using using Eqn.(2.3b)

$$
\begin{equation*}
\frac{2 R T_{c}}{\left(V_{c}-b\right)^{3}}-\frac{6 a}{V_{c}^{4}}=0 \tag{2.6}
\end{equation*}
$$



From Eqn.(2.5),

$$
\begin{equation*}
\frac{2 a}{V_{c}^{3}}=\frac{R T_{c}}{\left(V_{c}-b\right)^{2}} \tag{2.7}
\end{equation*}
$$

From Eqn.(2.6),

$$
\begin{equation*}
\frac{6 a}{V_{c}^{4}}=\frac{2 R T_{c}}{\left(V_{c}-b\right)^{3}} \tag{2.8}
\end{equation*}
$$

Using Eqns.(2.7) and (2.8), we get

$$
\begin{equation*}
b=\frac{V_{c}}{3} \tag{2.9}
\end{equation*}
$$

Substituting for $b$ from Eqn.(2.9) in (2.5)

$$
\frac{-R T_{c}}{\left(V_{c}-\frac{V_{c}}{3}\right)^{2}}+\frac{2 a}{V_{c}^{3}}=0
$$

i.e.,

$$
\frac{R T_{c}}{(4 / 9) V_{c}^{2}}=\frac{2 a}{V_{c}^{3}}
$$

giving,

$$
\begin{equation*}
a=\frac{9}{8} R T_{c} V_{c} \tag{2.10}
\end{equation*}
$$

Substituting for $a$ and $b$ from Eqns.(2.10) and (2.9) in Eqn.(2.2), and at critical conditions,

$$
\begin{aligned}
P_{c} & =\frac{R T_{c}}{V_{c}-V_{c} / 3}-\frac{9 / 8 R T_{c} V_{c}}{V_{c}^{2}} \\
& =\frac{3}{2} \frac{R T_{c}}{V_{c}}-\frac{9}{8} \frac{R T_{c}}{V_{c}}
\end{aligned}
$$

i.e.,

$$
P_{c}=\frac{3}{8} \frac{R T_{c}}{P_{c}}
$$

giving,

$$
\begin{equation*}
V_{c}=\frac{3}{8} \frac{K V_{c}}{P_{c}} \tag{2.11}
\end{equation*}
$$

Using Eqn.(2.11) in Eqns.(2.9) and (2.10), we get

$$
\begin{equation*}
a=\frac{27}{64} \frac{R^{2} T_{c}^{2}}{P_{c}} \tag{2.12}
\end{equation*}
$$

and

$$
\begin{equation*}
b=\frac{R T_{c}}{8 P_{c}} \tag{2.13}
\end{equation*}
$$

### 2.1.2 Derivation for $a$ and $b$ in another way

van der Waals equation is given as

$$
\left(P+\frac{a}{V^{2}}\right)(V-b)=R T
$$

Expanding the equation and rearranging, we get the following cubic equation for $V$ :

$$
\begin{equation*}
V^{3}-\left(b+\frac{R T}{P}\right) V^{2}+\frac{a}{P}-\frac{a b}{P}=0 \tag{2.14}
\end{equation*}
$$

Being a cubic equation, it has three roots for $V$. At $T=T_{c}$, all the three roots merge into one, i.e., $V_{c}$. i.e.,

$$
\left(V-V_{c}\right)^{3}=0
$$

Expanding the above,

$$
\begin{equation*}
V^{3}-3 V_{c} V^{2}+3 V_{c}^{2} V-V_{c}^{3}=0 \tag{2.15}
\end{equation*}
$$

Comparing the coefficients of Eqns.(2.14) and (2.15), at $T_{c}$ and $P_{c}$, we get

$$
\begin{align*}
3 V_{c} & =b+\frac{R T_{c}}{P_{c}}  \tag{2.16}\\
3 V_{c}^{2} & =\frac{a}{P_{c}}  \tag{2.17}\\
V_{c}^{3} & =\frac{a b}{P_{c}} \tag{2.18}
\end{align*}
$$

Eliminating $P_{c}$ from Eqns.(2.17) and (2.18), we get

$$
\begin{equation*}
b=\frac{V_{c}}{3} \tag{2.19}
\end{equation*}
$$

Substituting for $V_{c}$ using Eqn.(2.19), in Eqn.(2.16), we get,

$$
9 b=b+\frac{R T_{c}}{P_{c}}
$$

i.e.,

$$
\begin{equation*}
b=\frac{R T_{c}}{8 P_{c}} \tag{2.20}
\end{equation*}
$$

Substituting for $V_{c}$ using Eqn.(2.19), in Eqn.(2.17), we get

$$
3 \times(3 b)^{2}=\frac{a}{P_{c}}
$$

i.e.,

$$
\begin{equation*}
27 b^{2}=\frac{a}{P_{c}} \tag{2.21}
\end{equation*}
$$

Using Eqn.(2.20) in above equation, we get,

$$
\begin{equation*}
a=\frac{27}{64} \frac{R T_{c}^{2}}{P_{c}} \tag{2.22}
\end{equation*}
$$

## Redlich-Kwong Equation

$$
P=\frac{R T}{V-b}-\frac{a}{T^{1 / 2} V(V+b)}
$$

$$
\begin{aligned}
a & =\frac{0.42748 R^{2} T_{c}^{2.5}}{P_{c}} \\
b & =0.08664 \frac{R T_{c}}{P_{c}}
\end{aligned}
$$

## Berthelot Equation

$$
P=\frac{R T}{V-b}-\frac{a}{T V^{2}}
$$

$$
\begin{aligned}
a & =\frac{27}{64} \frac{R^{2} T_{c}^{3}}{P_{c}} \\
b & =\frac{R T_{c}}{8 P_{c}}
\end{aligned}
$$

## Dieterici Equation

$$
\begin{gathered}
P=\frac{R T}{V-b} \exp \left(\frac{-a}{R T V}\right) \\
a=\frac{4 R^{2} T_{c}^{2}}{P_{c} \exp (2)} \\
b=\frac{R T_{c}}{P_{c} \exp (2)}
\end{gathered}
$$

## S3n

### 26.2 The Dieterici equation

The van der Waals equation of state can be written in the form

$$
\begin{equation*}
p=p_{\text {repulsive }}+p_{\text {attractive }} \tag{26.31}
\end{equation*}
$$

where the first term is a repulsive hard sphere interaction

$$
\begin{equation*}
p_{\text {repulsive }}=\frac{R T}{V-b}, \tag{26.32}
\end{equation*}
$$

which is an ideal-gas-like term but with the denominator being the volume available to gas molecules, namely that of the container $V$ minus

## Blundell - Concepts in Thermal Physics.pdf

that of the molecules, $b$. The second term is the attractive interaction

$$
\begin{equation*}
p_{\text {attractive }}=-\frac{a}{V^{2}} \tag{26.33}
\end{equation*}
$$

There have been other attempts to model non-ideal gases. In the Berthelot equation, the attractive force is made temperature-dependent by writing

$$
\begin{equation*}
p_{\text {attractive }}=-\frac{a}{T V^{2}} \tag{26.34}
\end{equation*}
$$

Another approach is due to Dieterici, ${ }^{2}$ who in 1899 proposed an alternative equation of state in which he wrote thet

$$
\begin{equation*}
p=p_{\text {repulsive }} \exp \left(-\frac{a}{R T V}\right) \tag{26.35}
\end{equation*}
$$

and using eqn 26.32 this leads to

$$
\begin{equation*}
p\left(V_{\mathrm{m}}-b\right)=R T \exp \left(-\frac{a}{R T V_{\mathrm{m}}}\right) \tag{26.36}
\end{equation*}
$$

which is the Dieterici equation, here written in terms of the molar volume. The constant $a$ is, again, a parameter which controls the strength of attractive interactions. Isotherms of the Dieterici equation of state are shown in Fig. 26.7; they are similar to the ones for the van der Waals gas (Fig. 26.2), showing a very sudden increase in pressure as $V$ approaches b.
${ }^{2}$ Conrad Dieterici (1858-1929)


The critical point can be identified for this model by evaluating

$$
\begin{equation*}
\left(\frac{\partial^{2} p}{\partial V^{2}}\right)_{T}=\left(\frac{\partial p}{\partial V}\right)_{T}=0 \tag{26.37}
\end{equation*}
$$

and this yields (after a little atgebra)

$$
\begin{equation*}
T_{\mathrm{c}}=\frac{a}{4 R b}, \quad p_{\mathrm{c}}=\frac{a}{4 \mathrm{e}^{\frac{1}{2}} \overline{t_{2}, 2}}, \quad V_{\mathrm{c}}=2 b, \tag{26.38}
\end{equation*}
$$

for the critical temperature, pressure and volume, and hence

$$
\begin{equation*}
\frac{p_{\mathrm{c}} V_{\mathrm{c}}}{R T_{\mathrm{c}}}=\frac{2}{\mathrm{e}^{2}}=0.271 \tag{26.39}
\end{equation*}
$$

### 26.3 Virial expansion

Another method to model real gases is to take the ideal gas equation and modify it using a power series in $1 / V_{\mathrm{m}}$ (where $V_{\mathrm{m}}$ is the molar volume). This leads to the following virial expansion:

$$
\begin{equation*}
\frac{p V_{\mathrm{m}}}{R T}=1+\frac{B}{V_{\mathrm{it}}}+\frac{C}{V_{\mathrm{m}}^{2}}+\cdots \tag{26.40}
\end{equation*}
$$

In this equation, the parameters $B, C$, etc. are called virial coefficients and can be made to be temperature dependent (so that we will denote them by $B(T)$ and $C(T))$. The temperature at which the virial coefficient $B(T)$ goes to zero is called the Boyle temperature $T_{\mathrm{B}}$ since it is the temperature at which Boyle's law is approximately obeyed (neglecting the higher-order virial coefficients), as shown in Fig. 26.8.

### 26.4 The law of corresponding states

For different substances, the size of the molecules (which controls $b$ in the van der Waals model) and the strength of the intermolecular interactions (which controls $a$ in the van der Waals model) will vary, and hence their phase diagrams will be different. For example, the critical temperatures and pressures for different gases are different. However, the phase diagram of substances should be the same when plotted in reduced coordinates, which cain be obtained by dividing a quantity by its value at the critical point. Heace, if we replace the quantities $p, V, T$ by their reduced coordinates $\tilde{p}, \tilde{V}, Y^{\prime}$ defined by

$$
\begin{equation*}
\tilde{p}=\frac{p}{p_{\mathrm{c}}}, \quad \tilde{V}=\frac{V}{V_{\mathrm{c}}}, \quad \tilde{T}=\frac{T}{T_{\mathrm{c}}}, \tag{26.61}
\end{equation*}
$$

then phase diagrams of materials which are not wholly different from one another should lie on top of each other. This is called the law of corresponding states.

## Virial Equation

$$
\begin{aligned}
& z=1+B^{\prime} P+C P^{2}+D^{\prime} P^{3}+\cdots \\
& \text { or } \\
& z=1+\frac{B}{V}+\frac{C}{V^{2}}+\frac{D}{V^{3}}+\cdots
\end{aligned}
$$

## S3n

## Corresponding State Principle



S3n


$$
Z=f\left(T_{r}, P_{r}\right)
$$

To improve the accuracy of property predictions, Pitzer and coworkers introduced the acentric factor $\omega$ as a third correlating parameter.

$$
\begin{gathered}
Z=Z^{(0)}\left(T_{r}, P_{r}\right)+\omega Z^{(1)}\left(T_{r}, P_{r}\right) \\
\omega=-\left.\log _{10} P_{r}^{\text {sat }}\right|_{T_{r}=0.7}-1
\end{gathered}
$$


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The Lee/Kesler Generalized Correlation for the Compressibilty Factor

| $\mathbf{Z}^{\mathbf{0}}$ |  |  |  |  |  |  |  |  |  |
| :---: | :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| $\mathbf{T r}$ | $\mathbf{P r} \longrightarrow$ | $\mathbf{0 . 0 1}$ | $\mathbf{0 . 0 5}$ | $\mathbf{0 . 1 0}$ | $\mathbf{0 . 2 0}$ | $\mathbf{0 . 4 0}$ | $\mathbf{0 . 6 0}$ | $\mathbf{0 . 8 0}$ | $\mathbf{1 . 0 0}$ |
| $\boldsymbol{\downarrow}$ |  |  |  |  |  |  |  |  |  |
| $\mathbf{0 . 3 0}$ |  | 0.0029 | 0.0145 | 0.0290 | 0.0579 | 0.1158 | 0.1737 | 0.2315 | 0.2892 |
| $\mathbf{0 . 3 5}$ |  | 0.0026 | 0.0130 | 0.0261 | 0.0522 | 0.1043 | 0.1564 | 0.2084 | 0.2604 |
| $\mathbf{0 . 4 0}$ |  | 0.0024 | 0.0119 | 0.0239 | 0.0477 | 0.0953 | 0.1429 | 0.1904 | 0.2379 |
| $\mathbf{0 . 4 5}$ |  | 0.0022 | 0.0110 | 0.0221 | 0.0442 | 0.0882 | 0.1322 | 0.1762 | 0.2200 |
| $\mathbf{0 . 5 0}$ |  | 0.0021 | 0.0103 | 0.0207 | 0.0413 | 0.0825 | 0.1236 | 0.1647 | 0.2056 |
| $\mathbf{0 . 5 5}$ |  | 0.9804 | 0.0098 | 0.0195 | 0.0390 | 0.0778 | 0.1166 | 0.1553 | 0.1939 |
| $\mathbf{0 . 6 0}$ |  | 0.9849 | 0.0093 | 0.0186 | 0.0371 | 0.0741 | 0.1109 | 0.1476 | 0.1842 |
| $\mathbf{0 . 6 5}$ |  | 0.9881 | 0.9377 | 0.0178 | 0.0356 | 0.0710 | 0.1063 | 0.1415 | 0.1765 |
| $\mathbf{0 . 7 0}$ |  | 0.9904 | 0.9504 | 0.8958 | 0.0344 | 0.0687 | 0.1027 | 0.1366 | 0.1703 |
| $\mathbf{0 . 7 5}$ |  | 0.9922 | 0.9598 | 0.9165 | 0.0336 | 0.0670 | 0.1001 | 0.1330 | 0.1656 |
| $\mathbf{0 . 8 0}$ |  | 0.9935 | 0.9669 | 0.9319 | 0.8539 | 0.0661 | 0.0985 | 0.1307 | 0.1626 |
| $\mathbf{0 . 8 5}$ |  | 0.9946 | 0.9725 | 0.9436 | 0.8810 | 0.0661 | 0.0983 | 0.1301 | 0.1614 |
| $\mathbf{0 . 9 0}$ |  | 0.9954 | 0.9768 | 0.9528 | 0.9015 | 0.7800 | 0.1006 | 0.1321 | 0.1630 |
| $\mathbf{0 . 9 3}$ |  | 0.9959 | 0.9790 | 0.9573 | 0.9115 | 0.8059 | 0.6635 | 0.1359 | 0.1664 |

## Steam Tables

| Temp. ${ }^{\circ} \mathrm{C}$ T | $\begin{gathered} \text { Press. } \\ \mathbf{k P a}, \mathbf{M P a} \\ \boldsymbol{P} \end{gathered}$ | Specific Volume, $\mathrm{m}^{\mathbf{3} / \mathrm{kg}}$ |  | Internal Energy, kJ/kg |  |  | Enthalpy, kJ/kg |  |  | Entropy, kJ/kg |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Sat. Liquid $v_{f}$ | Sat. <br> Vapor $v_{R}$ | Sat. Liquid $\boldsymbol{u}_{f}$ | Evap. $u_{f g}$ | Sat. Vapor $u_{g}$ | Sat. Liquid $\boldsymbol{h}_{\boldsymbol{f}}$ | Evap. $h_{f k}$ | Sat. Vapor $h_{g}$ | Sat. Liquid $s_{f}$ | Evap. $s_{f k}$ |
| 0.01 T | 0.6113 | 0.001000 | 206.132 | 0.00 | 2375.3 | 2375.3 | 0.00 | 2501.3 | 2501.3 | 0.0000 | 9.1562 |
| 5 | 0.8721 | 0.001000 | 147.118 | 20.97 | 2361.3 | 2382.2 | 20.98 | 2489.6 | 2510.5 | 0.0761 | 8.9496 |
| 10 | 1.2276 | 0.001000 | 106.377 | 41.99 | 2347.2 | 2389.2 | 41.99 | 2477.7 | 2519.7 | 0.1510 | 8.7498 |
| 15 | 1.7051 | 0.001001 | 77.925 | 62.98 | 2333.1 | 2396.0 | 62.98 | 2465.9 | 2528.9 | 0.2245 | 8.5569 |
| 20 | 2.3385 | 0.001002 | 57.790 | 83.94 | 2319.0 | 2402.9 | 83.94 | 2454.1 | 2538.1 | 0.2966 | 8.3706 |
| 25 | 3.1691 | 0.001003 | 43.359 | 104.86 | 2304.9 | 2409.8 | 104.87 | 2442.3 | 2547.2 | 0.3673 | 8.1905 |
| 30 | 4.2461 | 0.001004 | 32.893 | 125.77 | 2290.8 | 2416.6 | 125.77 | 2430.5 | 2556.2 | 0.4369 | 8.0164 |
| 35 | 5.6280 | 0.001006 | 25.216 | 146.65 | 2276.7 | 2423.4 | 146.66 | 2418.6 | 2565.3 | 0.5052 | 7.8478 |
| 40 | 7.3837 | 0.001008 | 19.523 | 167.53 | 2262.6 | 24?9.1 | 167.54 | 2406.7 | 2574.3 | 0.5724 | 7.6845 |
| ......................................................................................................................... |  |  |  |  |  |  |  |  |  |  |  |
| 75 | 38.578 | 0.001026 | 4.131 | 313.87 | 2162.0 | 2475.9 | 313.91 | 2321.4 | 2635.3 | 1.0154 | 6.6670 |
| 80 | 47.390 | 0.001029 | 3.407 | 334.84 | 2147.4 | 2482.2 | 334.88 | 2308.8 | 2643.7 | 1.0752 | 6.5369 |
| 85 | 57.834 | 0.001032 | 2.828 | 355.82 | 2132.6 | 2488.4 | 355.88 | 2296.0 | 2651.9 | 1.1342 | 6.4102 |
| 90 | 70.139 | 0.001036 | 2.361 | 376.82 | 2117.7 | 2494.5 | 376.90 | 2283.2 | 2660.1 | 1.1924 | 6.2866 |
| 95 | 84.554 | 0.001040 | 1.982 | 397.86 | 2102.7 | 2500.6 | 397.94 | 2270.2 | 2668.1 | 1.2500 | 6.1659 |
| 100 | 0.10135 | 0.001044 | 1.6729 | 418.91 | 2087.6 | 2506.5 | 419.02 | 2257.0 | 2676.0 | 1.3068 | 6.0480 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 350 | 16.514 | 0.001740 | 0.008813 | 1641.81 | 776.6 | 2418.4 | 1670.54 | 893.4 | 2563.9 | 3.7776 | 1.4336 |
| 360 | 18.651 | 0.001892 | 0.006945 | 1725.19 | 626.3 | 2351.5 | 1760.48 | 720.5 | 2481.0 | 3.9146 | 1.1379 |
| 370 | 21.028 | 0.002213 | 0.004926 | 1843.84 | 384.7 | 2228.5 | 1890.37 | 441.8 | 2332.1 | 4.1104 | 0.6868 |
| 374.1CP 22.089 |  | 0.003155 | 0.003155 | 2029.58 | 0 | 2029.6 | 2099.26 | 0 | 2099.3 | 4.4297 | 0 |

## Single-phase tables

TABI.E. A.1.3SI Superheated Vapor Water (SI Units)

| $T$ | $P=10 \mathrm{kPa} \mathrm{(45.81)}$ |  |  |  | $P=50 \mathrm{kPa}(81.33)$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $v$ | $u$ | $h$ | $s$ | $v$ | $u$ | $h$ | $s$ |
| Sat. | 14.674 | 2437.9 | 2584.6 | 8.1501 | 3.240 | 2483.8 | 2645.9 | 7.593 |
| 50 | 14.869 | 2443.9 | 2592.6 | 8.1749 | - | - | - | - |
| 100 | 17.196 | 2515.5 | 2687.5 | 8.4479 | 3.418 | 2511.6 | 2682.5 | 7.694 |
| 150 | 19.513 | 2587.9 | 2783.0 | 8.6881 | 3.889 | 2585.6 | 2780.1 | 7.940 |
| 200 | 21.825 | 2661.3 | 2879.5 | 8.9037 | 4.356 | 2659.8 | 2877.6 | 8.157 |
| 250 | 24.136 | 2736.0 | 2977.3 | 9.1002 | 4.821 | 2735.0 | 2976.0 | 8.355 |
| 300 | 26.445 | 2812.1 | 3076.5 | 9. 2812 | 5.284 | 2811.3 | 3075.5 | 8.537 |

TABI.E A.1.4SI Compressed Liquid Water (SI Units)

| $T$ | $P=5.00 \mathrm{MPa}(263.99)$ |  |  |  | $P=10.00, \mathrm{MPa}(311.06)$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $v$ | $u$ | $h$ | $s$ | $v$ | $u$ | $h$ | $s$ |
| Sat. | . 0012859 | 1147.78 | 1154.21 | 2.9201 | . 0014524 | 1393.00 | 1407.53 | 3.354 |
| 0 | . 0009977 | 0.03 | 5.02 | 0.0001 | . 0009952 | 0.10 | 10.05 | 0.00 ( |
| 20 | . 0009995 | 83.64 | 88.64 | 0.2955 | . 0009972 | 83.35 | 93.32 | 0.29* |
| 40 | . 0010056 | 166.93 | 171.95 | 0.5705 | . 0010034 | 166.33 | 176.36 | 0.561 |
| 60 | . 0010149 | 250.21 | 255.28 | 0.8284 | . 0010127 | 249.34 | 259.47 | 0.82: |
| 80 | . 0010268 | 333.69 | 338.83 | 1.0719 | . 0010245 | 332.56 | 342.81 | 1.061 |
| 1 m | nninain | 41750 | 40271 | 13030 | 0010385 | 416.09 | 426.48 | 1.294 |


$537$
$T-v$ diagram for water


S3n

Two kilograms of water at $25^{\circ} \mathrm{C}$ are placed in a piston cylinder device under 3.2 MPa pressure as shown in the diagram (State (1)). Heat is added to the water at constant pressure until the temperature of the fluid reaches $350^{\circ} \mathrm{C}$ (State (2)). Determine the final volume of the fluid at state (2).

http://www.ohio.edu/mechanical/thermo/Intro/Chapt.1_6/Chapter2a.html

In this example since the pressure is known (3.2 MPa) and remains constant throughout the process, we find it convenient to draw a $P-v$ diagram indicating the process (1)-(2) as follows.


|  | $\mathbf{P}=3.0 \mathrm{MPa}\left(233.9^{\circ} \mathrm{C}\right)$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Temp | volume | energy | enthalpy | entropy |
| ${ }^{\circ} \mathrm{C}$ | $\mathrm{V}(\mathrm{m} \wedge 3 / \mathrm{kg})$ | u( $\mathrm{kJ} / \mathrm{kg}$ ) | h(kJ/kg) | $\mathrm{s}(\mathrm{kJ} / \mathrm{kg} . \mathrm{K})$ |
| Sat. | 0.0667 | 2603.2 | 2803.2 | 6.186 |
| 250 | 0.0706 | 2644.7 | 2856.5 | 6.289 |
| 300 | 0.0812 | 2750.8 | 2994.3 | 6.541 |
| 350 | 0.0906 | 2844.4 | 3116.1 | 6.745 |
| 400 | 0.0994 | 2933.5 | 3231.7 | 6.923 |
| 450 | 0.1079 | 3021.2 | 3344.8 | 7.086 |
| 500 | 0.1162 | 3108.6 | 3457.2 | 7.236 |
| 600 | 0.1325 | 3285.5 | 3682.8 | 7.510 |
| 700 | 0.1484 | 3467.0 | 3912.2 | 7.759 |
| 800 | 0.1642 | 3654.3 | 4146.9 | 7.989 |
| 900 | 0.1799 | 3847.9 | 4387.5 | 8.203 |
| 1000 | 0.1955 | 4047.7 | 4634.1 | 8.405 |


| $\mathbf{P}=\mathbf{3 . 5 ~ M P a}\left(242.6^{\circ} \mathrm{C}\right)$ |  |  |  |
| ---: | ---: | ---: | ---: |
| volume | energy | enthalpy | entropy |
| $v\left(\mathrm{~m}^{\wedge} 3 / \mathrm{kg}\right)$ | $u(\mathrm{~kJ} / \mathrm{kg})$ | $\mathrm{h}(\mathrm{kJ} / \mathrm{kg})$ | $\mathrm{s}(\mathrm{kJ} / \mathrm{kg} . \mathrm{K})$ |
| 0.0571 | 2602.9 | 2802.6 | 6.124 |
| 0.0588 | 2624.0 | 2829.7 | 6.176 |
| 0.0685 | 2738.8 | 2978.4 | 6.448 |
| 0.0768 | 2836.0 | 3104.8 | 6.660 |
| 0.0846 | 2927.2 | 3223.2 | 6.843 |
| 0.0920 | 3016.1 | 3338.0 | 7.007 |
| 0.0992 | 3104.5 | 3451.6 | 7.159 |
| 0.1133 | 3282.5 | 3678.9 | 7.436 |
| 0.1270 | 3464.7 | 3909.3 | 7.685 |
| 0.1406 | 3652.5 | 4144.6 | 7.916 |
| 0.1541 | 3846.4 | 4385.7 | 8.130 |
| 0.1675 | 4046.4 | 4632.7 | 8.332 |

http://www.ohio.edu/mechanical/thermo/property tables/H2O/H2O Super3.html (18-Aug-2012)

We find that we need to interpolate between pressure $P=3.0 \mathrm{MPa}$ and $\mathrm{P}=3.5 \mathrm{MPa}$ in order to determine the specific volume at the required pressure of 3.2 MPa as follows:

| Superheat Vapor Tables |  |  |  |
| :--- | :---: | :---: | :---: |
| P | 3.0 | 3.2 | 3.5 |
| T | MPa |  |  |
| $\mathrm{V} @ 350^{\circ} \mathrm{C}$ | $233.9^{\circ} \mathrm{C}$ | $237.4^{\circ} \mathrm{C}$ | $242.6^{\circ} \mathrm{C}$ |
|  | 0.0906 | 0.085 | 0.0768 |
| m 3 |  |  |  | kg

$$
\left.\begin{array}{l}
\xrightarrow[(242.6-233.9)^{\circ} \mathrm{C}]{\left(\mathrm{T}_{\text {sat }}-233.9{ }^{\circ} \mathrm{C}\right.} \frac{(3.2-3.0)}{(3.5-3.0)} \mathrm{MPa} \\
\quad \Rightarrow \mathrm{~T}_{\text {sat }}=237.4^{\circ} \mathrm{C}
\end{array}\right]=0.4 \mathrm{Ma} .
$$

From the corresponding state principle by considering $Z$ as a function of ( $T_{r}, P_{r}$ ) estimate the volume of 1 kmol of oxygen at 200 K and 6 x $10^{6} \mathrm{~N} / \mathrm{m}^{2} .\left(P_{c}=5.05 \times 10^{6} \mathrm{~N} / \mathrm{m}^{2} ; T_{c}=155 \mathrm{~K}\right)$. $Z$ values for various $T_{r}$, $P_{r}$ are as given below:

|  | $Z$ |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
| $T_{r}$ | $P_{r} \rightarrow$ | $\mathbf{0 . 8}$ | $\mathbf{1 . 0}$ | $\mathbf{1 . 2}$ |
| $\mathbf{1 . 1}$ | 0.7649 | 0.6880 | 0.5984 | 0.4580 |
| $\mathbf{1 . 2}$ | 0.8330 | 0.7858 | 0.7363 | 0.6605 |
| $\mathbf{1 . 3}$ | 0.8764 | 0.8438 | 0.8111 | 0.7624 |
| $\mathbf{1 . 4}$ | 0.9062 | 0.8827 | 0.8595 | 0.8256 |
| $\mathbf{1 . 5}$ | 0.9278 | 0.9103 | 0.8933 | 0.8689 |

First by considering the interpolation at fixed values of Pr, get $Z$; then at fixed $\operatorname{Tr}$ value get the $Z$.
That way, you will get $\mathbf{Z}$ as $\mathbf{0 . 8 0 7}$

